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Localized knowledge spillovers and patent citations: A distance-based approach*

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Abstract

We develop a new approach to localized knowledge spillovers by incorporating the concept of control patents (Jaffe, Trajtenberg and Henderson 1993) into the distance-based test of localization (Duranton and Overman, 2005). Using microgeographic data, we identify localization distance while allowing for cross-boundary spillovers, unlike the existing literature where the extent of localized knowledge spillovers is detected at the state or metropolitan statistical area level. We revisit the recent debate by Thompson and Fox-Kean (2005) and Henderson, Jaffe and Trajtenberg (2005) on the existence of localized knowledge spillovers, and find solid evidence supporting localization, even when finer controls are used.

Keywords: localized knowledge spillovers; distance-based tests; microgeographic data; K -density; patent citations; control patents

JEL classifications: O31; R12

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1 Introduction

Ever since Marshall (1920), it is widely recognized that knowledge spillovers are one of the three major determinants of industry agglomeration. Of the three determinants given in his classic book, intellectual spillovers are harder to identify than trade in goods and labor pooling (Ellison, Glaeser and Kerr, 2010). Nonetheless, Jaffe, Trajtenberg and Henderson (1993) developed a matching rate method to test localized knowledge spillovers as evidenced by patent citations. By controlling for the preexisting geographic concentration of production, they found evidence supporting localized knowledge spillovers at the state and metropolitan statistical area (MSA) levels. However, their finding was recently challenged by Thompson and Fox-Kean (2005). The major difference between these two studies lies in the selection of control patents. In Jaffe, Trajtenberg and Henderson (1993), control and citing patents share a technology class at the three-digit level, whereas in Thompson and Fox-Kean (2005), both patents share a finer technology subclass at the six-digit level.¹ The latter authors further restricted to control patents that have any subclass code in common with originating patents, and found no evidence supporting localized knowledge spillovers at the state and MSA levels. The existence of localized knowledge spillovers is, thus, still inconclusive (Henderson, Jaffe and Trajtenberg, 2005).

Are states and MSAs relevant spatial units for testing localized knowledge spillovers? There is no *a priori* reason for the extent of knowledge spillovers to be limited by administrative boundaries. The matching rate approach, taken by Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005), however, is silent on this issue because it allocates inventors to states and MSAs while abstracting from where those aggregated spatial units are located on the map. Put differently, their approach makes the distance from Boston, MA, to New Haven, CT, equivalent to that of Boston, MA, to Los Angeles, CA.² To capture possible cross-boundary knowledge spillovers, we conduct distance-based tests of localization that have been recently developed by Duranton and Overman (2005). Their basic idea is to generate the distribution of distances between pairs of establishments in an industry and to compare it with that of hypothetical industries, in which establishments are randomly allocated across existing establishment sites, in order to assess the significance of departures from randomness.

We apply the distance-based approach to test whether knowledge spillovers, as evidenced

¹These case-control methods have been applied to detect localized knowledge spillovers in numerous contexts for almost two decades. See Almeida (1996) for an early application to the U.S. semiconductor industry. More recent contributions include Agrawal, Kapur and McHale (2008) and Agrawal, Cockburn and Rosell (2010), in which they explored innovation in company towns and the role of ethnicity in knowledge flows.

²It should also be noted that spatial units often differ in population and area, so that spatial aggregations tend to mix different spatial scales. For instance, localization tests at the state level involve comparisons between Rhode Island and California, whose area is more than 150 times as large. Furthermore, such aggregation often leads to spurious correlations across aggregated variables, which is known as the Modifiable Areal Unit Problem (MAUP).

by patent citations, are localized, and examine to what extent they are localized (if they are). In doing so, we consider which technology classes are localized, and identify the class-specific localization distance.³ Our key idea is to use citation distances, computed from inventors' addresses at the census place level, instead of distances between establishments in Duranton and Overman (2005). We generate the distribution of citation distances by allowing for the fact that citing–cited relationships are unidirectional, unlike the establishment data. Our novelty lies in incorporating the concept of control patents and the construction of counterfactuals in a consistent way. This can be done by randomly drawing counterfactual citations, as in Duranton and Overman (2005), while controlling for the existing geographic concentration of technological activities, as in Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005). We finally detect localized knowledge spillovers by comparing the actual and counterfactual distributions of citation distances. We thus build a new bridge between these two different strands of literature. To our knowledge, there has so far been no attempt to apply the distance-based method to citing–cited relationships.

Our main results can be summarized as follows. First, distance matters. Our distance-based tests find that, even when we use six-digit controls, knowledge spillovers are localized significantly for about one-third of all 360 technology classes in question. This is in sharp contrast to Thompson and Fox-Kean (2005) who used six-digit controls and found no evidence supporting localized knowledge spillovers at the state and MSA levels. In the three-digit case, more than 70% of 384 technology classes in question exhibit localization, thus confirming the result by Jaffe, Trajtenberg and Henderson (1993). We further show that, in both cases, the majority of technology classes displaying localization are localized at least once within 200 km, which corresponds roughly to the distance between Boston and New Haven, for example. We also find that more than 95% of all technology classes exhibiting localization are localized within 1200 km, which constitutes an upper bound of knowledge spillovers.

Second, heterogeneity across technology classes also matters. In particular, our six-digit analysis reveals that, while about one-third of technology classes exhibit localization, more than 10% of technology classes display dispersion. This, together with the six-digit result in Thompson and Fox-Kean (2005), implies that aggregating different technology classes can offset the tendency toward localization even when a substantial number of technology classes display localization at the disaggregate level.

The biases from aggregating spatial units and technology classes are shown to be substantial. To explore the difference between the matching rate and distance-based approaches in detecting localized knowledge spillovers, we conduct class-specific matching rate tests, and compare the number of localized classes with the corresponding number generated by our distance-based tests. It turns out that, although the numbers are roughly the same for the

³As shown in Ellison and Glaeser (1997) and Duranton and Overman (2005), the degree of *industry* localization is known to differ across industries. Thus, we would quite naturally expect that the extent of knowledge spillovers can also differ across technology classes, and we show that this is indeed the case.

three-digit case, the matching rate tests underestimate the number of localized classes for the six-digit case. Indeed, the matching rate tests fail to detect localized knowledge spillovers for more than 60% of the technology classes that exhibit localization by the distance-based tests.

Hence, our analysis, which allows for distance and heterogeneity across technology classes, has rich implications for knowledge cluster policies: relevant technology classes must be chosen, i.e., classes that display significant localization should be carefully selected; and cross-boundary knowledge spillovers need to be taken into account, i.e., inventors who benefit from positive knowledge externalities must be clustered in a borderless manner. Our analysis further suggests that the timing of policies must also be determined accurately because the number of localized technology classes and the associated localization distances can change over time.

The rest of the paper is organized as follows. Section 2 describes data and methodology. Section 3 reports our main results. Section 4 concludes.

2 Data and Methodology

This section describes data and methodology. Unlike the conventional matching rate tests at the state and MSA levels, we need to combine patent citations data and microgeographic data to conduct distance-based tests. Concerning methodology, we first identify control patents, as in Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005), to control for the existing geographic distribution of technological activities. We then construct counterfactuals, as in Duranton and Overman (2005), while using the case-control methods. The counterfactual citations thus obtained, with which we compare the actual citations to detect localized knowledge spillovers, share common features between the matching rate and the distance-based tests. Hence, we can make a direct comparison between these two tests for localization.

2.1 Patents and Patent Citations

Our data are based on the NBER U.S. Patent Citations Data File, which is described in detail by Hall, Jaffe and Trajtenberg (2001). This data set covers all patent applications between 1963 and 1999 and those granted by 1999, as well as citing–cited relationships for patents granted between 1975 and 1999. For each patent, the list of inventors, addresses of inventors, and the technological category are recorded, along with other information such as year of application, assignees, and the type of assignees. The detailed information of patent application month and *patent class* (three-digit) and *subclass* (six-digit) codes is supplemented with the United States Patent and Trademark Office (USPTO) Patent BIB database.⁴

We begin with 142,245 U.S. nongovernmental patents that were granted between January 1975 and December 1979. The sampling period is chosen to be comparable to those of previous

⁴We use the patent classification as of December 31, 1999.

studies. We identify patents as “U.S.” if the country of the assignee is the United States. We observe that 115,905 (81.5%) of them were cited at least once by other U.S. patents, and we call them the *originating patents*. We then identify the *citing patents* that cited the originating patents by examining all patents that were granted between January 1975 and December 1999. We further exclude “self-citations”. A citing patent is classified as self-citing (i) if it had the same assignee as the originating patent that it cited; or (ii) if it was invented by the same inventor as the originating patent that it cited.⁵ To distinguish unique inventors, we use the computerized matching procedure (CMP) proposed by Trajtenberg, Shiff and Melamed (2006).⁶ The CMP uses not only the name of inventors recorded in the patents, but also patent citations, and inventors’ addresses, while allowing for possible errors in names. We find that 15.0% of citing patents are classified as self-citations. After excluding self-citations, we obtain 647,983 citing patents.

2.2 Geographic Information

Our distance-based approach to localized knowledge spillovers requires microgeographic data, namely the locations at which inventions were created. In this paper, we identify the location of each invention at the census place level. The U.S. Census Bureau defines a place as a concentration of population. There are 23,789 places in the 1990 census, which we use below.⁷ They are much more finely delineated than counties (there are 3,141 counties), but not as small as zip code areas (there are 29,470 zip code areas).⁸ Figure 1 shows the boundary map of census places for the contiguous U.S. area.

Insert Figure 1

To be more specific, restricting patent inventors who reside in the contiguous U.S. area, we first match the address of each inventor to the 1990 census place by their names. If the name match fails, we locate it via the populated place provided by the U.S. Geographic Names Information System (GNIS). We match the inventor’s address with the GNIS populated place,

⁵Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005) regard only the former as self-citations. Our criterion (ii) rules out spurious knowledge spillovers associated with inventor mobility. Furthermore, in response to the comments by Henderson, Jaffe and Trajtenberg (2005), we exclude control patents that share the same inventors or the same assignees with the originating patents.

⁶See Nakajima, Tamura and Hanaki (2010) for the implementation detail of the CMP.

⁷In the 1990 census, there are two major types of places: census designated places (CDPs); and incorporated places. These data can be obtained from 1990 U.S. Gazetteer Files.

⁸We could use zip code areas. The NBER U.S. Patent Citations Data File, however, reports zip codes for only 15.4% of all U.S. patent records. As the NBER Data File reports cities for almost all cases, we could relate cities to zip codes. Yet, it is often the case that a city has several to dozens of zip codes. Also, the area for each zip code as of 1990, which is needed to compute its internal distance below, is not available. We therefore decided to link cities with census places whose relationships are uniquely determined and whose areas as of 1990 are readily available.

which is more finely delineated than the census place, and then find the census place that is nearest to the identified GNIS populated place by using their spatial coordination information. This procedure allows us to identify the 18,139 census places for 97.0% of all inventors in the sample. The average of within-area distances for census places is 1.70 km, which is far smaller than those for counties (22.60 km), Consolidated Metropolitan Statistical Areas (CMSAs) (59.93 km), and states (197.93 km).⁹

2.3 Control Patents and Counterfactuals

Since industries generally tend to agglomerate with one another, the mere geographic coincidence of originating and citing patents does not provide solid support for localized knowledge spillovers. For example, in the semiconductor industry, many citations are concentrated in Silicon Valley. This need not imply localized knowledge externalities. It may just reflect the fact that a disproportionate fraction of firms of the related technological area is located in that region. Hence, to test localized knowledge spillovers, we must control for the existing geographic distribution of technological activities.

To this end, we use *control patents*, proposed by Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005), which satisfy the following two conditions. First, control patents should belong to the same *technological area* as the citing patent under consideration. Jaffe, Trajtenberg and Henderson (1993) selected a control patent at the *three-digit* level, whereas Thompson and Fox-Kean (2005) constructed a finer control at the *six-digit* level. The latter also claimed that a control should match not only with the citing patent but also with the originating patent. In what follows, emphasizing their difference in technology classification, we refer to the controls of Jaffe, Trajtenberg and Henderson (1993) as the *three-digit controls*, and call those of Thompson and Fox-Kean (2005) the *six-digit controls*. Second, a control patent should be in the same cohort as the citing patent. Jaffe, Trajtenberg and Henderson (1993) chose a control patent whose application date is within a one-month window on either side of the citing patent's application date. Similarly, Thompson and Fox-Kean (2005) set the application date of a control patent within plus-or-minus six month around that of the citing patent. Following these studies, we use one-month and six-month windows for the three-digit and six-digit controls, respectively.¹⁰

Insert Table 1

⁹These distances are computed by the formula derived by Kendall and Moran (1963), which is presented in Section 2.5.

¹⁰There is one minor difference between their and our control patents. We use a fixed application date window within which control patents are searched, while Thompson and Fox-Kean (2005) enlarge it in incremental steps from a one-month window, then a three-month window, and, if necessary, a six-month window until the control patent is found for each citing patent.

Table 1 presents the sample sizes. The first column shows the total numbers of the originating and citing patents. These numbers include patents with and without controls. In the second and third columns, the numbers of originating and citing patents having at least one control are reported. It should be noted that citing patents do not always have controls, and, even if they do, the control is not necessarily unique for each citing patent. As shown, 60.20% of the citing patents have three-digit controls. The rate of the citing patents having six-digit controls is lower, at 18.65%. The citing patents with no controls assigned (and their originating patents) are dropped out of the samples.¹¹ As a result, 92.64% of the originating patents remain “in-sample” for the three-digit controls, and the corresponding number is 51.04% for the six-digit controls. In the analysis that follows, we use these in-sample patents.

Once the relevant control patents are identified, we can construct *counterfactuals* with which we compare the actual citations. For each citation, we define an admissible patent set by collecting the citing and control patents, either three or six digit, so that the admissible patent set consists of the patents that either actually cited or *could have cited* the originating patent. We then allocate a counterfactual citation between the originating patent and a patent that is randomly drawn from the corresponding admissible patent set.¹² In what follows, we propose tests that nonparametrically balance the actual and counterfactual citations subject to the same technological and temporal profiles, and attribute the remaining difference in geographic distributions to the localization of knowledge spillovers, which is unrelated to the preexisting concentration of technological activities.

2.4 The Matching Rate Approach

The main idea of the matching rate approach, invented by Jaffe, Trajtenberg and Henderson (1993) and refined by Thompson and Fox-Kean (2005), is to compute the geographic matching rate of the actual citations, and compare it with that of counterfactual citations. Following the previous studies, we define the matching rate of the actual citations as the proportion of the citing patents whose geographic units such as states and CMSAs are matched with those of the originating patents. We analogously define the matching rate of the counterfactual citations by matching geographic units between an originating patent and a patent that is randomly drawn from the corresponding admissible patent set. Thompson and Fox-Kean (2005) propose a similar random sampling method to construct the matching rate of the

¹¹We also drop technology classes in which originating patents are distributed across less than 10 census places. This selection of patents is required because we estimate the density of distances for each technology class in the subsequent analysis, and a sufficient number of location points are needed to obtain well-behaved estimated density functions. See Section 3.2 for more exposition.

¹²It should be noted that, in the six-digit case, we use the admissible patent set that consists only of the citing and control patents belonging to the same technology class as the corresponding originating patent. This is a logical consequence of the additional restriction in the six-digit case that originating-citing-control triads of patents must share at least one patent subclass in common.

counterfactual citations. They randomly select a patent from the admissible patent set *once* for each citation. By contrast, we resample patents *many times* from the admissible patent set, and consider a simulated distribution of the counterfactual matching rate. We now describe the procedure of our matching rate test in detail.

Let p^c be the population probability that a citing patent is in the same geographic unit as the originating patent, and let p^r be the corresponding probability for a randomly drawn patent from the admissible patent set. We test the null hypothesis $H_0 : p^c = p^r$ (no localized knowledge spillovers) against the alternative hypothesis $H_1 : p^c > p^r$ (significant localized knowledge spillovers). Let \hat{p}^c be the matching rate of the actual citations that we observe in the data. Under the null hypothesis, it is not statistically different from a realization of the counterfactual matching rate, which we denote by \hat{p}^r . We thus reject the null hypothesis of no localized knowledge spillovers if the p -value, $\text{Prob}(\hat{p}^c \leq \hat{p}^r)$, is less than 5%.

We first construct the observed matching rate \hat{p}^c as follows. Let $\{o^i\}_{i=1}^{n^o}$ be the set of originating patents, where n^o is the number of originating patents. The set of the patents that cite o^i is defined as $\{c^{ij}\}_{j=1}^{n^{ci}}$, where n^{ci} is the number of citing patents. We compute the number of location matches, m^{ci} , between the originating patent o^i and the citing patents $\{c^{ij}\}_{j=1}^{n^{ci}}$. The total number of location matches divided by the total number of citations gives the observed matching rate $\hat{p}^c = \sum_{i=1}^{n^o} m^{ci} / \sum_{i=1}^{n^o} n^{ci}$.

We then construct the distribution of the counterfactual matching rate \hat{p}^r by the following Monte Carlo simulation. For each citing patent c^{ij} , we identify the admissible patent set R^{ij} that consists of the citing patent itself and the associated control patents. Suppose that we run 1000 simulations. In the k -th simulation, for each citing patent c^{ij} , we randomly select a hypothetical patent r_k^{ij} from the admissible patent set R^{ij} . We then calculate the number of location matches, m_k^{ri} , between the originating patent o^i and the randomly chosen hypothetical patents $\{r_k^{ij}\}_{j=1}^{n^{ci}}$. The total number of location matches divided by the total number of hypothetical citations gives the counterfactual matching rate $\hat{p}_k^r = \sum_{i=1}^{n^o} m_k^{ri} / \sum_{i=1}^{n^o} n^{ci}$, where the total number of hypothetical citations equals that of actual citations. The Monte Carlo process allows us to obtain the simulated distribution of the matching rate $\{\hat{p}_k^r\}_{k=1}^{1000}$. We finally compute the p -value of the matching rate test by using the standard percentile method.

Although the matching rate test is straightforward, one should be careful for multiple inventors per patent. To determine whether or not a pair of citing and cited patents falls into the same geographic unit, we use the following two matching methods. Consider, for each citing-cited relationship, all possible pairs of an inventor of the citing patent and an inventor of the cited patent. The locations of the citing and cited patents are then matched (i) if the majority of all possible inventor pairs fall into the same geographic unit (*median* matching); or (ii) if at least one pair of inventors falls into the same geographic unit (*minimum* matching). These matching methods are in accord with those used in previous studies. For example, Jaffe, Trajtenberg and Henderson (1993) employ a similar method as our median matching. Thompson and Fox-Kean (2005) mention the minimum matching as an alternative to their

random matching.

2.5 The K -density Approach

As mentioned in the Introduction, the extent of knowledge spillovers is unlikely to be limited by administrative boundaries. The matching rate approach that we have taken in the previous subsection, however, cannot address this issue because it abstracts from where CMSAs and states are located in the United States. To capture possible cross-boundary knowledge spillovers, we rely on distance-based tests of localization that were recently developed by Duranton and Overman (2005). Their basic idea is to generate the distribution of distances between pairs of establishments in an industry and to compare it with that of hypothetical industries, in which establishments are randomly allocated across existing establishment sites, in order to assess the significance of departures from randomness.

We apply Duranton and Overman’s approach to test whether knowledge spillovers, as evidenced by patent citations, are localized, and examine to what extent they are localized (if they are). As before, we allocate a counterfactual citation between the originating patent and a patent drawn randomly from the corresponding admissible patent set. Unlike the matching rate approach, however, we compare the distribution of *distances* between the originating and citing patents with the counterfactual distribution generated by the randomization. We then consider the deviation from randomness as evidence of localized knowledge spillovers. Our distance-based test uses the same counterfactuals as the matching rate test, so that we can make a direct comparison between these two tests for localization. We thus build a new bridge between the two strands of literature, which are the matching rate test of localized knowledge spillovers and the distance-based test of industry localization.

Such an attempt, however, poses two main difficulties that we need to deal with. First, unlike establishments whose locations are usually uniquely determined, patents can have multiple addresses because their inventors are not necessarily unique. We thus compute, for each citation relationship, all possible distances between the inventors of the originating patent and those of the citing patent, and focus on their median or minimum distance. The distance computation is in line with the median or minimum matching method of the matching rate tests, respectively, as presented above. We do the same for the counterfactual citation relationship.

Second, because of the data limitation, the location of each inventor is identified at the census place level. Although census places are narrowly delineated compared with counties and states, they are not spatial points. This poses a “zero distance” problem, i.e., even when the actual distance between the originating and citing inventors is not zero, it is measured to be zero if they happen to live in the same census place. To address this problem, we consider spatial interaction between the two inventors within the same census place. Assuming that each census place is a circle, it is readily verified that the distance between the two randomly chosen points in a census place with area S is given by $[128/(45\pi)]\sqrt{S/\pi}$ (Kendall and Moran,

1963). We use this correction for the distance between the two inventors who are in the same census place, instead of regarding the distance as to be zero.

It is also noted that, unlike the previous studies on patent citations, we analyze the localization distance that is specific to each patent class. Because the degree of localization is known to differ across industries (e.g., Ellison and Glaeser, 1997; Duranton and Overman, 2005), it seems natural to expect that the extent of localized knowledge spillovers can also differ across patent classes. As we show later, this is indeed the case.

We now describe the detailed procedure of our distance-based test of localized knowledge spillovers. Let \mathcal{A} be the set of all technology classes, categorized at the patent class level. We denote by $\{o_A^i\}_{i=1}^{n_A^o}$ the set of originating patents for technology class $A \in \mathcal{A}$, where n_A^o is the number of originating patents. The set of patents that cite o_A^i is denoted by $\{c_A^{ij}\}_{j=1}^{n_A^{ci}}$, where n_A^{ci} is the number of citing patents. The number of citations originating from technology class A is then given by $N_A = \sum_{i=1}^{n_A^o} n_A^{ci}$. We finally denote by d_A^{ij} the great-circle distance between patents o_A^i and c_A^{ij} , which, as mentioned above, is given by either the minimum or median distance from the inventors of the originating patent to those of the citing patent. Following Duranton and Overman (2005), the kernel density (henceforth K -density) estimator of citation distance for technology class A at any point d is

$$\widehat{K}_A(d) = \frac{1}{2hN_A} \sum_{i=1}^{n_A^o} \sum_{j=1}^{n_A^{ci}} f\left(\frac{d - d_A^{ij}}{h}\right), \quad (1)$$

where f is a Gaussian kernel function and h is the bandwidth set as in Silverman (1986). Note that, expression (1) reflects the fact that, unlike Duranton and Overman (2005), we consider unidirectional relationships from the inventors of originating patents to those of citing patents.¹³

Concerning counterfactuals, we run 1000 Monte Carlo simulations.¹⁴ The construction of counterfactuals is the same as that of the matching rate test. For each citing patent c_A^{ij} , we identify the admissible patent set R_A^{ij} that consists of the citing patent itself and the associated control patents. In each simulation, we randomly draw a hypothetical patent r_{Ak}^{ij} from the admissible patent set R_A^{ij} for each citing patent c_A^{ij} to estimate the counterfactual K -density for the distribution of distances from originating patents o_A^i to hypothetical patents r_{Ak}^{ij} , using a formula similar to (1). After 1000 simulation runs, we rank the counterfactual densities at each 10 km in ascending order and select the 5-th and the 95-th percentiles to obtain a lower 5% and an upper 5% confidence interval that we denote $\overline{K}_A(d)$ and $\underline{K}_A(d)$, respectively.

Detecting localization based on $\overline{K}_A(d)$ and $\underline{K}_A(d)$, however, only allows us to make local statements at a given distance. Unfortunately, this does not lead to statements about the

¹³As in Duranton and Overman (2005), we adopt the reflection method in Silverman (1986) to deal with boundary problems associated with the fact that distances cannot be negative.

¹⁴We also repeated our simulations 2000, 5000, and 10,000 times for several technology classes, and obtained very similar results.

global citation patterns of a technology class because even a technology class with randomly distributed citations will exhibit dispersion or localization with a high probability. Indeed, by construction, there is a 5% probability that a technology class displays localization for each distance, so that the probability for this to occur at least once across all distances is quite high.

Therefore, we finally define the global confidence bands that we use to detect localized knowledge spillovers. Let \bar{d}_A be the maximum distance for technology class A under consideration.¹⁵ We look for the identical upper and lower local confidence intervals such that, when we consider them *across all distances* between 0 and \bar{d}_A km, only 5% of our randomly generated K -densities hit them. Let $\overline{\overline{K}}_A(d)$ be the upper global confidence band of technology class A . When $\widehat{K}_A(d) > \overline{\overline{K}}_A(d)$ for at least one $d \in [0, \bar{d}_A]$, this technology class is said to exhibit *global localization* at a 5% confidence level. Conversely, the lower global confidence band of technology class A , $\underline{\underline{K}}_A(d)$, is such that it is hit by 5% of the randomly generated K -densities that are not localized. A technology class is then said to exhibit *global dispersion* at a 5% confidence level when $\widehat{K}_A(d) < \underline{\underline{K}}_A(d)$ for at least one $d \in [0, \bar{d}_A]$ and the technology class does not exhibit global localization. The definition of global dispersion requires no global localization because otherwise dispersion at large distances could be a consequence of localization at smaller distances, given that our densities must sum to one by construction. Hence, we define

$$\Gamma_A(d) \equiv \max \left\{ \widehat{K}_A(d) - \overline{\overline{K}}_A(d), 0 \right\}$$

as an index of global localization, and

$$\Psi_A(d) \equiv \begin{cases} \max \left\{ \underline{\underline{K}}_A(d) - \widehat{K}_A(d), 0 \right\} & \text{if } \sum_d \Gamma_A(d) = 0 \\ 0 & \text{otherwise} \end{cases}$$

as an index of global dispersion.

Insert Figure 2

Figures 2(a)–(b) illustrate K -densities (solid) and global confidence bands (dotted) for two patent classes, namely butchering (452) and amusement devices: toys (446), respectively. The former exhibits global localization while the latter is globally dispersed.

3 Results

The purpose of this section is fourfold. Using the matching rate tests *at the aggregate level*, we first replicate the same qualitative features as those of Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005), despite some differences in data and methodology. We

¹⁵Following Duranton and Overman (2005), we define the maximum distance as the median of all distances of all possible counterfactual citations for technology class A .

then turn to our K -density tests, and show that a substantial number of technology classes display localization, even when control patents are selected at the six-digit level. We further explore in details why the discrepancy arises between these two tests by comparing our class-specific distance-based tests with the matching rate tests *at the disaggregate level*. We finally derive some policy implications from our findings.

3.1 The Matching Rate Tests

Table 2 reports the results of the matching rate tests for the state, CMSA and county levels.¹⁶ Following Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005), the matching rate tests are implemented *at the aggregate level* encompassing all technology classes. Using controls at the three- and six-digit levels, we compare the observed matching rate with the average of the counterfactual matching rates for each geographic unit. The standard errors of the counterfactual matching rates are computed by simulation with 1000 replications.

Insert Table 2

In the case of the three-digit controls, the observed matching rates are significantly higher than the counterfactual ones for all spatial scales, although the matching rates become smaller for finer geographic units. We reject the null hypothesis of no localized knowledge spillovers at a 5% significance level, and, thus, find solid evidence of localized knowledge spillovers. By contrast, the null hypothesis is not rejected for the six-digit controls, which suggests no evidence of localized knowledge spillovers. These results share the same qualitative features as those of Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005), although our data construction and methodology are somewhat different from theirs.

3.2 The K -density Tests

We now describe the results of the K -density tests. We introduce some notations. For a technology class $A \in \mathcal{A}$, knowledge spillovers are said to exhibit *localization at distance d* if $\Gamma_A(d) > 0$, whereas they are said to exhibit *dispersion at distance d* if $\Psi_A(d) > 0$. We define a technology class A as having localized knowledge spillovers if $\Gamma_A \equiv \sum_d \Gamma_A(d) > 0$, and as having dispersed knowledge spillovers if $\Psi_A \equiv \sum_d \Psi_A(d) > 0$. Finally, we use $L^1 = \{A \in \mathcal{A} | \Gamma_A > 0\}$ and $D^1 = \{A \in \mathcal{A} | \Psi_A > 0\}$ to denote the sets of technology classes displaying localized and dispersed knowledge spillovers, respectively.

Table 3 presents the main results. As we consider both the minimum and median distances, as well as the three- and six-digit controls, there are four possibilities. First, concerning the three-digit case, we find localized knowledge spillovers for the majority of technology classes, with about 70% being localized for both the median and minimum distances. These results

¹⁶As in Thompson and Fox-Kean (2005), we use 16 CMSAs as defined in 1981 by excluding Puerto Rico.

are in line with those obtained by Jaffe, Trajtenberg and Henderson (1993). Turning to the six-digit controls, more than 30% of technology classes exhibit localized knowledge spillovers regardless of whether we use the median or minimum distance. Although fewer classes exhibit localization in the six-digit case, we obtain solid evidence for localized knowledge spillovers. This is surprising given that Thompson and Fox-Kean (2005) find no evidence supporting localization at the state and CMSA levels. The matching rate tests that we have presented above also report no localization for the six-digit controls.

Insert Table 3

To investigate more closely the scope of knowledge spillovers, let $L^1(d) = \{A \in \mathcal{A} | \Gamma_A(d) > 0\}$ and $D^1(d) = \{A \in \mathcal{A} | \Psi_A(d) > 0\}$ be the sets of technology classes that exhibit localization and dispersion, respectively. Figure 3 illustrates the distributions of $|L^1(d)|$ and $|D^1(d)|$ for the three- and six-digit controls. In each case, there is no substantial difference between the median (solid) and the minimum (dotted) distance methods. We see that the number of localized technology classes is greater at smaller distances for both the three- and six-digit controls. The degree of localization decreases as the distance from the originating patents increases, thus suggesting that knowledge spillovers decay with distance. Interestingly, this is consistent with the assumption that is made in the recent theory of spatial development (Desmet and Rossi-Hansberg, 2009). By contrast, there is no clear pattern for dispersed knowledge spillovers, although we observe some significant dispersion across various distances. Such dispersion of citing inventors may arise, for instance, when the benefits of their pooling is dominated by the costs of their poaching from firms' perspectives (Combes and Duranton, 2006).

Insert Figure 3

We can delineate a boundary within which knowledge spillovers are localized. Figure 4 shows the percentages of technology classes displaying localization at least once within distance d . As shown, there are substantial differences between the three- and six-digit cases. However, no matter which control is used, more than half of the technology classes displaying localized knowledge spillovers are localized at least once within about 200 km, which corresponds roughly to the distance between Boston and New Haven. We can also consider 1200 km as an upper bound of the extent of knowledge spillovers because more than 95% of all localized classes are localized by this distance, regardless of which controls are used.

Insert Figure 4

We further examine heterogeneity in the patterns of knowledge spillovers across technology classes. Figure 5 illustrates the distributions of Γ_A and Ψ_A for the median distance case because the results are fairly robust regardless of the choice between the median and the minimum distances.¹⁷ Both distributions are skewed substantially with the localization and

¹⁷The results of the minimum distance method are available upon request from the authors.

dispersion indices being close to zero, while there are several technology classes displaying highly localized or dispersed knowledge spillovers. Interestingly, for the three-digit controls, the fraction of localized technology classes outweighs substantially that of dispersed technology classes. By contrast, in the six-digit case, the corresponding difference between the localized and dispersed technology classes is not so large.

Insert Figure 5

Finally, Table 4 presents the top 20 technology classes with highest degrees of localization, measured by Γ_A , for the median distance case. The rankings for the three- and six-digit controls are roughly similar, in that five out of the top 20 localized classes overlap between the three- and six-digit cases.¹⁸ Table 4 also shows that knowledge spillovers are highly localized in “traditional” industries such as: agriculture, husbandry and food (Patent Class 452); furniture and house fixtures (256); earth working and wells (166 and 405); and apparel and textile industries (2, 36, and 112), where the categories are given by Hall, Jaffe and Trajtenberg (2001). We also find significant localization of knowledge spillovers for many mechanical industries (Patent Classes 192, 221, 239, 254, 296, 301, 303, 411, 440, 492 and 508), in particular, transportation mechanical industries (296 and 301).

Insert Table 4

3.3 Comparison

We have shown that, unlike the matching rate tests, the K -density tests provide solid evidence for localized knowledge spillovers, even for the six-digit controls. We now explore the differences, as well as the similarities, in detecting localization between these two approaches. In particular, we argue, in what follows, that the matching rate tests using the six-digit controls underestimate localization of knowledge spillovers because of the following two “aggregation” problems.

The first problem is “technological aggregation”. As shown above, the K -density tests reveal considerable heterogeneity across technology classes in whether knowledge spillovers are localized or dispersed. This is particularly so, in the six-digit case, where the distributions of Γ_A and Ψ_A are roughly similar. Accordingly, if these heterogeneous classes are pooled, as in the conventional matching rate tests, both localization and dispersion can be cancelled out with each other, and, thus, may leave no evidence of localization at the aggregate level.

To confirm this idea, we implement *class-specific* matching rate tests. Specifically, we test the hypothesis of no localized knowledge spillovers at the 5% significance level *for each technology class*. Let $L_1 = \{A \in \mathcal{A} | p_A^c > p_A^r\}$ denote the set of technology classes that exhibit

¹⁸In fact, the rank correlation coefficient between the three- and six-digit controls is computed as $\rho = 0.36$, and the null hypothesis of no correlation is rejected at the 1% significance level.

localization by the class-specific matching rate tests, where p^c and p^r depend on technology class A . Table 5 shows that, when the three-digit controls are used, localized knowledge spillovers are detected for 270 or 266 technology classes, depending on whether the spatial units are states or CMSAs. Interestingly, these numbers are fairly close to the 275 localized classes, obtained from the K -density tests in Table 3.¹⁹ Hence, we conclude that the matching rate and the K -density tests detect roughly the same number of localized technology classes for the three-digit controls.

However, for the six-digit controls, the matching rate and the K -density tests substantially differ in detecting the number of localized technology classes. Indeed, the class-specific matching rate tests identify localization for a smaller fraction of technology classes than do the K -density tests. More concretely, only 47 to 69 technology classes display localization in the former tests, depending on the spatial units, whereas more than 100 technology classes are shown to be localized in the latter tests. Yet, even in the class-specific matching rate, the percentages of technology classes with localized knowledge spillovers remain in the range between 13% and 20%. Hence, we find evidence that knowledge spillovers are localized for nonnegligible, though not overwhelming, technology classes, even in the six-digit case.

Insert Table 5

The second problem of the conventional matching rate tests is “geographic aggregation”. The matching rate tests *ex ante* allocate inventors to spatial units such as states and CMSAs. As Duranton and Overman (2005) pointed out, this aggregation treats administrative units symmetrically, so that inventors in neighboring spatial units are treated in exactly the same way as inventors at the opposite ends of a country. This creates a downward bias when dealing with localized knowledge spillovers that cross an administrative boundary. The distance-based tests have an advantage in that they do not overlook such cross-border knowledge flows.

To investigate this possibility, we again focus on the discrepancy between the matching rate and the K -density tests for the six-digit controls. We first implement the matching rate tests for the two groups of technology classes, that is, the set of localized technology classes by the K -density tests, $L^1 = \{A \in \mathcal{A} | \Gamma_A > 0\}$, and the set of nonlocalized technology classes, $L^0 = \{A \in \mathcal{A} | \Gamma_A = 0\}$. We then define $L_0^1 = \{A \in \mathcal{A} | p_A^c = p_A^r \text{ and } \Gamma_A > 0\}$ as the set of technology classes where the K -density tests detect significant localization, while the matching rate tests do not. Thus, it follows that $L_0^1 \subseteq L^1$. Similarly, we define $L_1^0 = \{A \in \mathcal{A} | p_A^c > p_A^r \text{ and } \Gamma_A = 0\} \subseteq L^0$.

Table 6 provides the results. First, looking at the results of $|L_0^1|$ in the first and second rows, a large number of technology classes that are detected as localized by the K -density tests are not identified as localized by the matching rate tests. We thus find that the matching rate

¹⁹Table 5 shows the results for the median matching case. The results for the minimum matching case are qualitatively similar, and, thus, are omitted. They are available upon request from the authors.

tests *underestimate* localized knowledge spillovers. The number of underestimated technology classes ranges from 67 to 89, depending on the spatial units. These biases are substantial since the percentage of underestimated classes is as high as 61% to 62% at the state and CMSA levels, respectively, and it amounts to 81% at the county level. Moving to the results of $|L_1^0|$ in the third and fourth rows, a number of technology classes that are not detected as localized by the K -density tests are identified as localized by the matching rate tests. This implies that the matching rate tests can also *overestimate* localized knowledge spillovers. However, the numbers of *underestimated* localized classes, $|L_0^1|$, much outweigh those of *overestimated* localized classes, $|L_1^0|$. We see that the difference ranges from 40 to 62, which explains the difference between $|L^1|$ in Table 3 and $|L_1|$ in Table 5 for the six-digit controls.

Insert Table 6

We finally investigate where we observe the downward biases of the matching rate tests using the six-digit controls in detecting localized knowledge spillovers. Figure 6 plots $|L_0^1(d)|$ for each distance d , where $L_0^1(d) = \{A \in \mathcal{A} | p_A^c = p_A^r \text{ and } \Gamma_A(d) > 0\}$. We first notice that the downward biases tend to be most substantial around 200 km or 500 km, depending on whether we focus on counties or on CMSAs and states. For example, the county-level matching rate tests fail to detect about 40 technology classes as having no localized knowledge spillovers at 200 km. This underestimation is inherent in their construction. The matching rate tests cannot discern, by their definitions, knowledge spillovers that travel longer than their predetermined administrative boundaries. For example, given that the average of within-area distances for the U.S. states is 197.9 km, localized knowledge spillovers whose scope significantly exceeds that distance are unlikely to be captured by the state-level matching rate test. In this light, the matching rate tests with smaller spatial units, which have the smaller average of within-area distances, tend to more severely underestimate localized knowledge spillovers that can be detected by the K -density tests.

Insert Figure 6

In summary, the existing matching rate tests systematically understate localized knowledge spillovers, as evidenced by patent citations. We explain this by two aggregation problems, which are technological and geographic aggregations. If we control for heterogeneity in localization and dispersion by disaggregating technology classes, the matching rate tests provide evidence of localized knowledge spillovers for a fraction of technology classes. Yet, they still fail to identify a substantial number of localized technology classes that are detected by the distance-based K -density tests. Our analysis also suggests that the matching rate tests with smaller administrative units tend to exacerbate the underestimation problem. In view of this, the geographic aggregation problem with the matching rate tests cannot be resolved, even when taking smaller administrative units such as counties. Rather, in that case, the downward biases become more substantial.

3.4 Policy implications

Our K -density tests find solid evidence supporting localization, regardless of whether we use the three- or six-digit controls. Since we allow for distance and heterogeneity across technology classes, our findings shed new light on cluster policies. First, policy makers need to select the “right” technology classes, i.e., those displaying significant localized knowledge spillovers. Second, for each “right” technology class, the “right” scope, i.e., the distance within which the technology class exhibits localization, must also be selected in a borderless manner. Since the majority of technology classes that display localization are localized within 200 km, knowledge cluster policies can generally be made within this distance in order to enhance knowledge externalities.

However, this is not the end of the story. The combination of the “right” technology class and the “right” scope at one time does not necessarily ensure a successful cluster policy at other times. For instance, the father of Silicon Valley, Frederick Terman, could not replicate “Silicon Valley East” in New Jersey several years later. The reason why such an attempt, led by Bell Laboratories, was in vain, may be that they failed to choose “right” time, as pointed out by Findlay (1992) and Leslie and Kargon (1996). This experience suggests that “right” technology classes and “right” scopes may change over time.

To explore this issue, we restrict ourselves to the citing patents granted in two sub-periods, 1985-1989 and 1995-1999. Interestingly, Figure 7 illustrates that, as time goes by, the number of localized technology classes, $|L^1(d)|$, gets smaller in shorter distances while it gets larger in longer distances. This feature is common to the three- and six-digit cases, although it is less clear in the latter case. We further show that, in both cases, the distances within which the majority of technology classes displaying localization are localized can increase up to 500 km in the latter period. It should be noted, however, that the larger the cluster size the more likely to be higher the commuting costs and land rents. Accordingly, such large-scale cluster policies are unlikely to be justified by the cost-benefit analysis that encompasses not only positive knowledge externalities but also negative congestion externalities, as emphasized by Duranton et al. (2010). Hence, we may conclude that policy makers must also care about the “right” time to implement cluster policies.

Insert Figure 7

4 Conclusion

We propose a distance-based approach to localized knowledge spillovers and revisit the recent debate by Thompson and Fox-Kean (2005) and Henderson, Jaffe and Trajtenberg (2005) on the existence of localized knowledge spillovers. Our concern has been two aggregation problems, namely technological and geographic aggregations, both of which are ignored in that

literature. Overcoming these two problems, our distance-based tests have found solid evidence supporting localized knowledge spillovers for a substantial number of technology classes, even when the finer six-digit controls are used. At the same time, nonnegligible technology classes exhibit dispersion, thus implying considerable heterogeneity across classes. We show that the class-specific matching rate tests for the six-digit controls understate the number of localized technology classes that are detected by the distance-based tests. These aggregation biases may thus explain why the matching rate tests, implemented by Thompson and Fox-Kean (2005), could not find any significant evidence for intranational knowledge spillovers.

Our distance-based tests have found that the number of localized technology classes for the six-digit controls is smaller than that for the three-digit controls. However, as argued by Henderson, Jaffe and Trajtenberg (2005), finer controls need not be better because they can induce the sample selection problem. Our six- and three-digit results thus provide the possible shares of localized technology classes, with the range being between 30% and 70%. Furthermore, we show that, in either case, the localization of knowledge spillovers attenuates with distance. We thus conclude that substantial numbers of technology classes display localized knowledge spillovers at the intranational level, regardless of whether we use the three- or six-digit controls.

To compare our distance-based tests with the conventional matching rate tests such as Jaffe, Trajtenberg and Henderson (1993) and Thompson and Fox-Kean (2005), we have relied on typical case-control methods by specifying the technology level at which control patents are selected. It is worth noting, however, that Thompson (2006) developed an alternative method that does not involve such case controls. Using more recent data that can distinguish citations added by inventors from those added by examiners, Thompson (2006) showed that inventor citations are more likely to match the state or CMSA of their originating patents than examiner citations. Given our result that the matching rate tests are subject to the two aggregation problems, that alternative approach may be biased as well. Our distance-based method can be modified to address such an issue by testing for the localization of inventor added citations *relative to* the counterfactual geographic distribution of examiner added citations.

Our findings from class-specific distance-based tests have several implications for cluster policies. First, policy makers need to select the “right” technology classes. Second, for each “right” technology class, the “right” scope must also be taken into account. Since the majority of technology classes that display localization are localized within 200 km, knowledge cluster policies can generally be made within this distance in order to enhance knowledge externalities. As administrative boundaries need not limit knowledge spillovers, such policies would require coordination among adjacent administrative units. Last, policy makers must also care about the “right” time to implement cluster policies because the “right” technology classes and the “right” scopes can change over time. Although we have mainly focused on cross-boundary knowledge spillovers to illustrate the biases generated by the matching rate tests, our K -density tests can also be applied to localized knowledge clusters in smaller scales. This direction is

independently explored by Kerr and Kominers (2010).²⁰

Finally, our distance-based measure of localized knowledge spillovers can be used to explore the determinants of industry agglomeration. Some studies (e.g., Rosenthal and Strange, 2001; Ellison, Glaeser and Kerr, 2010) already attempted to include proxies for the importance of knowledge spillovers, which are constructed more directly from patent data, into their regression analysis. However, we are not aware of any study that incorporates a measure of *localized* knowledge spillovers for explaining industry agglomeration. Using such a localization measure would lead to a better understanding of the relationship between industry agglomeration and knowledge spillovers.

²⁰We became aware of their project after the first draft of our paper was completed. Kerr and Kominers (2010) apply a similar distance-based method to patent data. However, there is one notable difference. Their K -density tests detect localization by comparing pairwise distances among inventors in a technology with those obtained from 1000 random draws of U.S. inventors of a similar size to that technology, as have been done by Duranton and Overman (2005) in the context of establishment agglomeration. Hence, their K -density tests abstract from the concept of control patents and explicit citing-cited relationships, both of which are at the heart of our tests.

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Table 1: Sample Patent Sizes

	Total	3-digit	6-digit
Originatings	115,905	107,561	59,168
Percent	(100.00)	(92.64)	(51.04)
Citings	647,983	390,104	120,876
Percent	(100.00)	(60.20)	(18.65)
Controls	—	33,472,826	941,532

Table 2: Matching Rate Test Results

		3-digit Control		6-digit Control	
		Median	Minimum	Median	Minimum
State	Observed Rate (%)	12.53*	13.54*	13.38	14.31
	Counterfactual Rate (%)	9.33	10.16	13.45	14.49
	Std. Error	(0.04)	(0.04)	(0.07)	(0.06)
CMSA	Observed Rate (%)	9.24*	10.29*	10.12	11.18
	Counterfactual Rate (%)	6.54	7.32	10.33	11.37
	Std. Error	(0.03)	(0.03)	(0.06)	(0.06)
County	Observed Rate (%)	4.08*	5.27*	4.34	5.62
	Counterfactual Rate (%)	2.54	3.31	4.63	5.88
	Std. Error	(0.02)	(0.02)	(0.04)	(0.05)

Notes: * denotes statistically significant at 5% level.

Table 3: K -density Test Results

	3-digit Control		6-digit Control	
	Median	Minimum	Median	Minimum
All Classes $ \mathcal{A} $	384	384	360	360
Localized Classes $ L^1 $	275	273	109	109
Non-localized Classes $ L^0 $	109	111	251	251
Dispersed Classes $ D^1 $	39	40	41	51
$ L^1 / \mathcal{A} \times 100$ (percent)	(71.61%)	(71.09%)	(30.27%)	(30.28%)

Table 4: Top 20 Localized Technology Classes

Class ID	Patent Class Name	Γ_A	Overlapped
3-digit controls			
405	Hydraulic and Earth Engineering	0.0201	■
452	Butchering	0.0155	
36	Boots, Shoes, and Leggings	0.0153	
223	Apparel Apparatus	0.0145	
606	Surgery	0.0143	
367	Communications, Electrical: Acoustic Wave Systems and Devices	0.0135	
296	Land Vehicles: Bodies and Tops	0.0122	■
285	Pipe Joints or Couplings	0.0106	■
492	Roll or Roller	0.0103	
181	Acoustics	0.0100	
30	Cutlery	0.0098	
501	Compositions: Ceramic	0.0095	
411	Expanded, Threaded, Driven, Headed, Tool-Deformed, or Locked-Threaded Fastener	0.0089	■
254	Implements or Apparatus for Applying Pushing or Pulling Force	0.0088	
256	Fences	0.0087	■
239	Fluid Sprinkling, Spraying, and Diffusing	0.0082	
290	Prime-Mover Dynamo Plants	0.0081	
303	Fluid-Pressure and Analogous Brake Systems	0.0078	
192	Clutches and Power-Stop Control	0.0078	
112	Sewing	0.0077	
6-digit controls			
256	Fences	0.0070	■
221	Article Dispensing	0.0038	
248	Supports	0.0030	
433	Dentistry	0.0029	
222	Dispensing	0.0025	
137	Fluid Handling	0.0024	
141	Fluent Material Handling, with Receiver or Receiver Coacting Means	0.0023	
296	Land Vehicles: Bodies and Tops	0.0023	■
301	Land Vehicles: Wheels and Axles	0.0023	
405	Hydraulic and Earth Engineering	0.0022	■
440	Marine Propulsion	0.0022	
411	Expanded, Threaded, Driven, Headed, Tool-Deformed, or Locked-Threaded Fastener	0.0022	■
166	Wells	0.0022	
285	Pipe Joints or Couplings	0.0022	■
508	Solid Anti-Friction Devices, Materials Therefor, Lubricant or Separate Compositions for Moving Solid Surfaces, and Miscellaneous Mineral Oil Compositions	0.0021	
2	Apparel	0.0020	
261	Gas and Liquid Contact Apparatus	0.0019	
198	Conveyors: Power-Driven	0.0019	
218	High-Voltage Switches with Arc Preventing or Extinguishing Devices	0.0019	
118	Coating Apparatus	0.0018	

Table 5: Matching Rate Test Results for Disaggregated Technology Classes

	3-digit controls			6-digit controls		
	State	CMSA	County	State	CMSA	County
All Classes $ \mathcal{A} $	384	384	384	360	360	360
Localized Classes $ L_1 $	270	266	247	68	69	47
Non-localized Classes $ L_0 $	114	118	137	292	291	313
$ L_1 / \mathcal{A} \times 100$ (percent)	(70.31%)	(69.27%)	(64.32%)	(18.89%)	(19.17%)	(13.06%)

Table 6: Matching Rate Tests Conditional on K -density Tests for Six-digit Controls

	State	CMSA	County
$ L_0^1 : p_A^c = p_A^r$ and $\Gamma_A > 0$	67	68	89
$ L_0^1 / L^1 \times 100$ (percent)	(61.47%)	(62.39%)	(81.65%)
$ L_1^0 : p_A^c > p_A^r$ and $\Gamma_A = 0$	26	28	27
$ L_1^0 / L^0 \times 100$ (percent)	(10.36%)	(11.16%)	(10.76%)

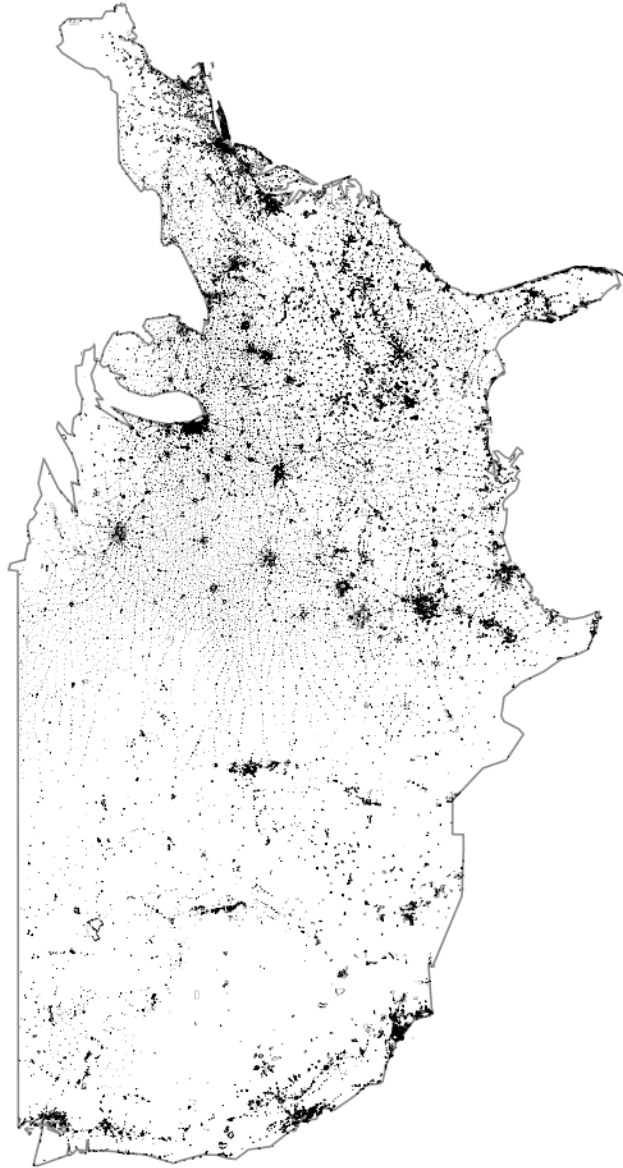


Figure 1: Census Places as of 1990

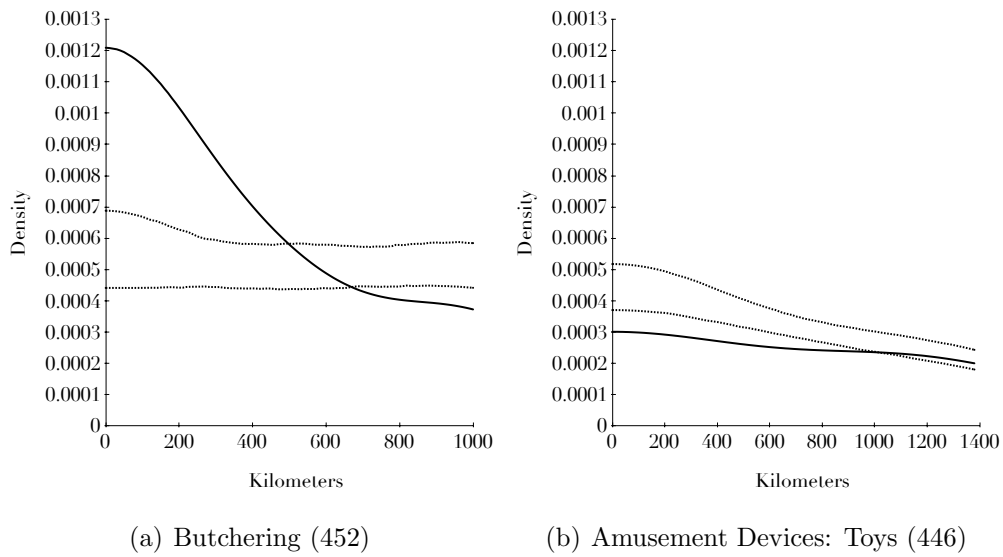


Figure 2: K -density and Global Confidence Bands for Two Illustrative Patent Classes

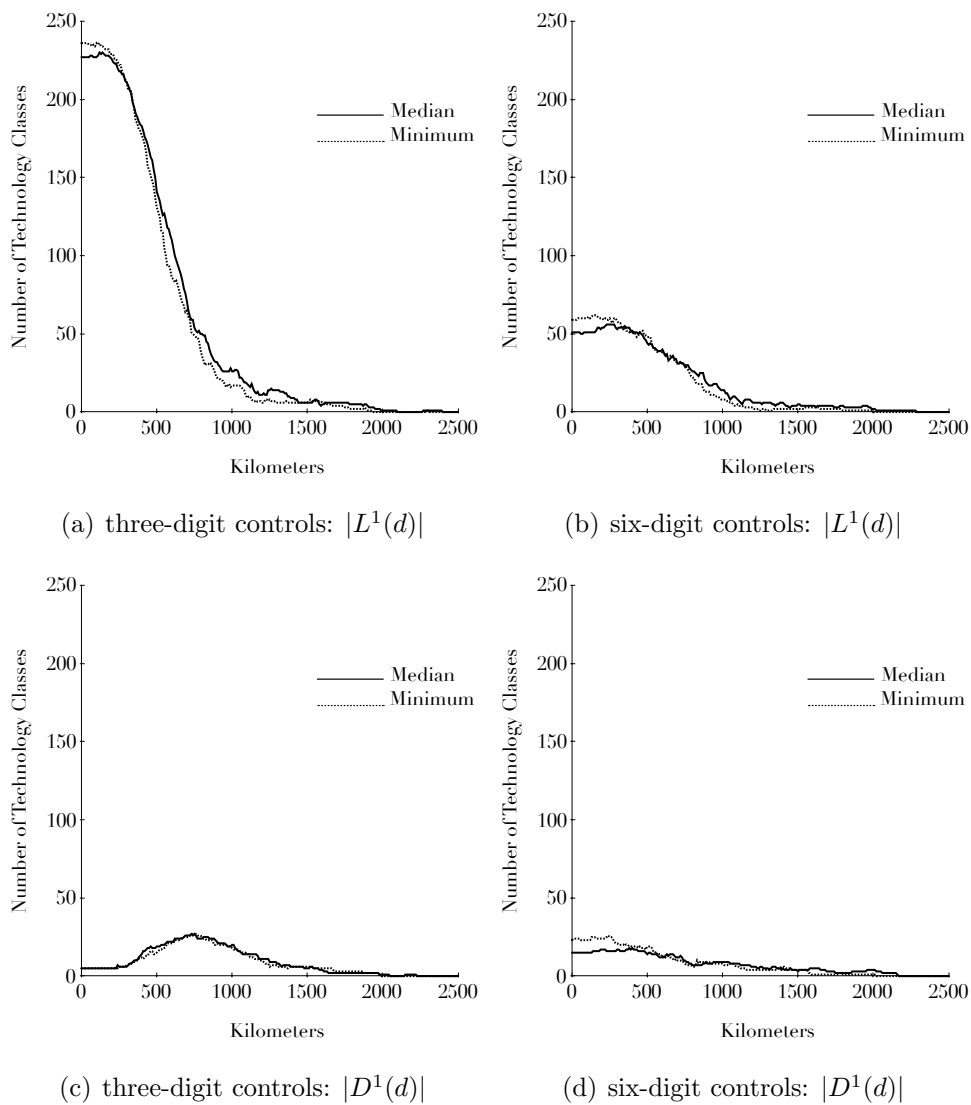


Figure 3: Distance Distribution of the Numbers of Technology Classes

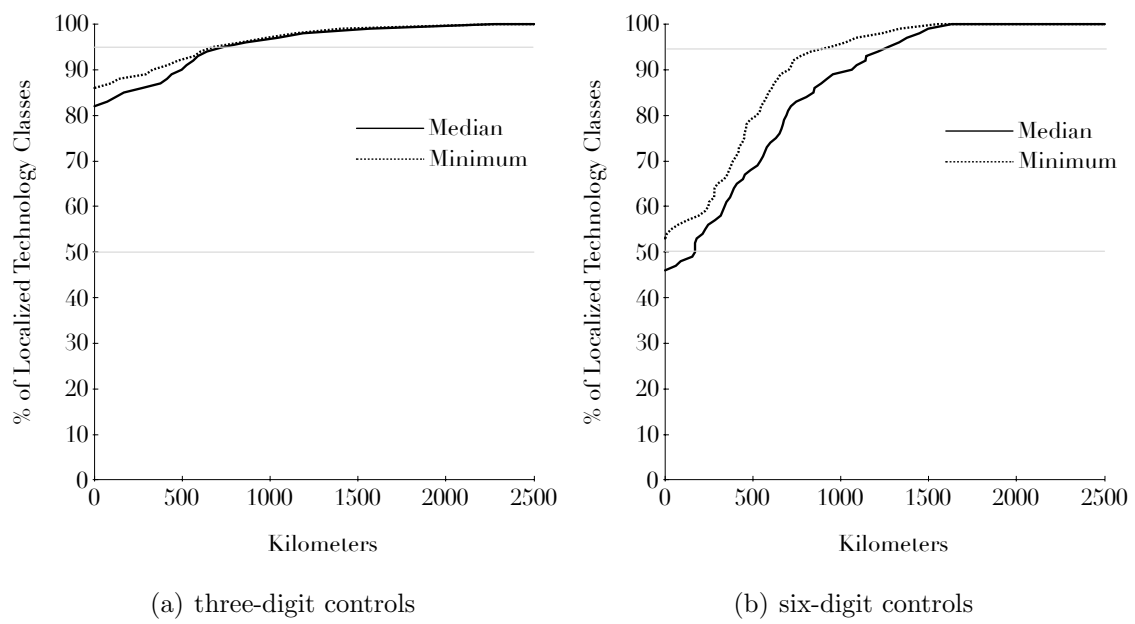


Figure 4: Percentage of Localized Technology Classes within Each Distance

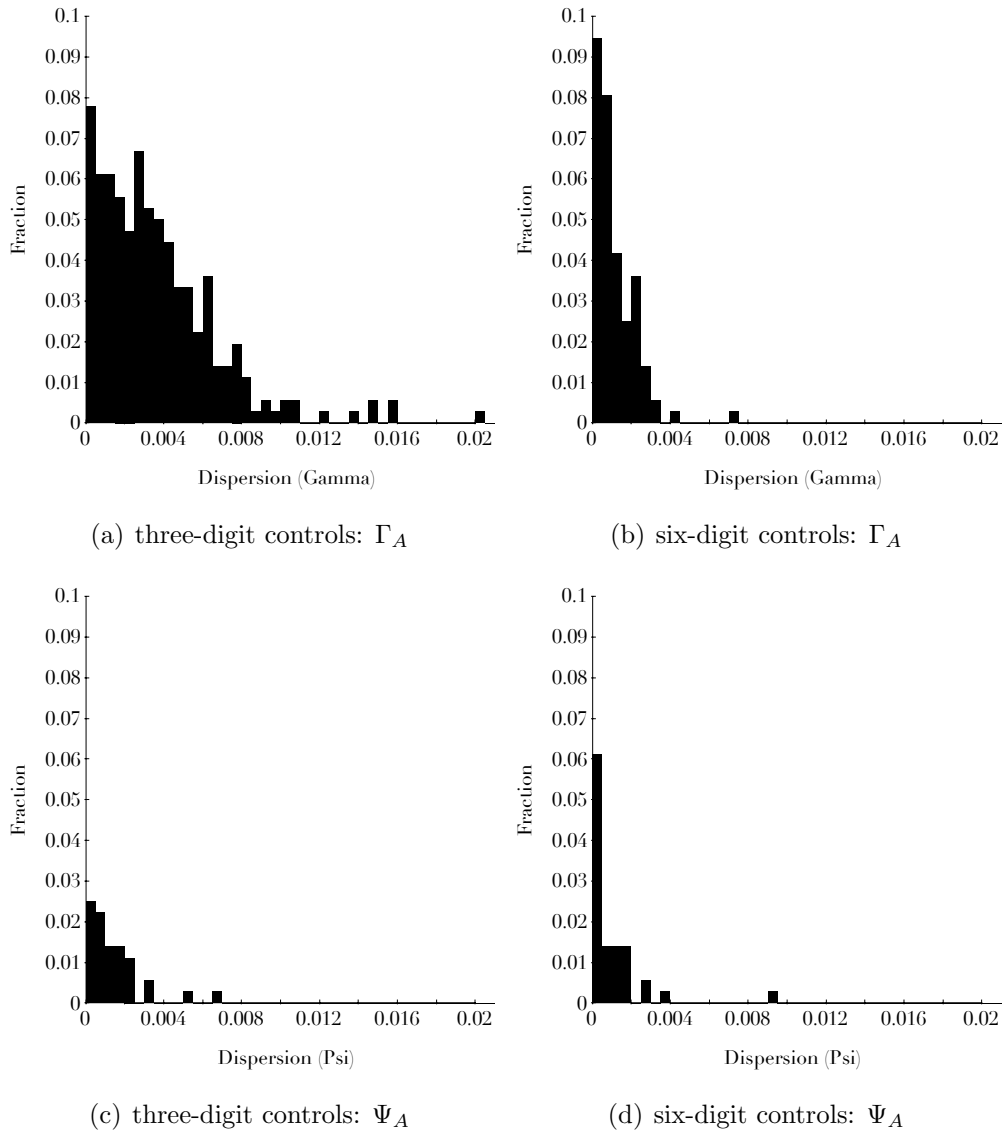


Figure 5: Distributions of Localization and Dispersion Indices

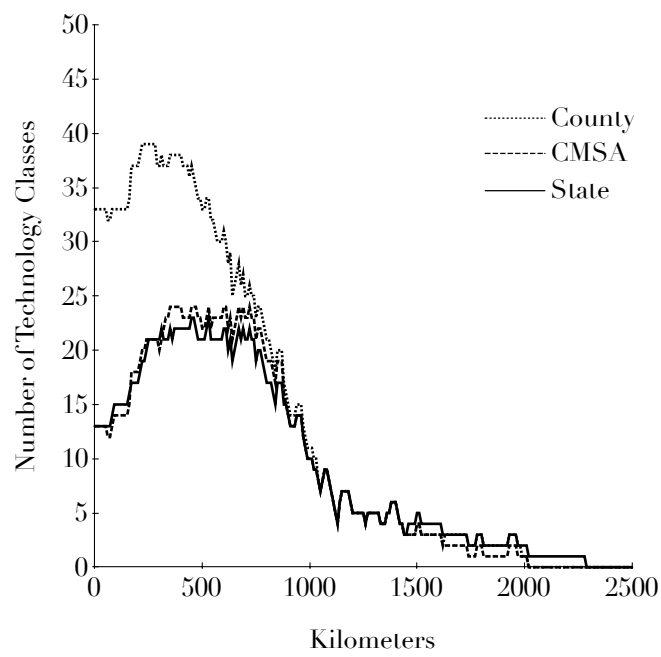
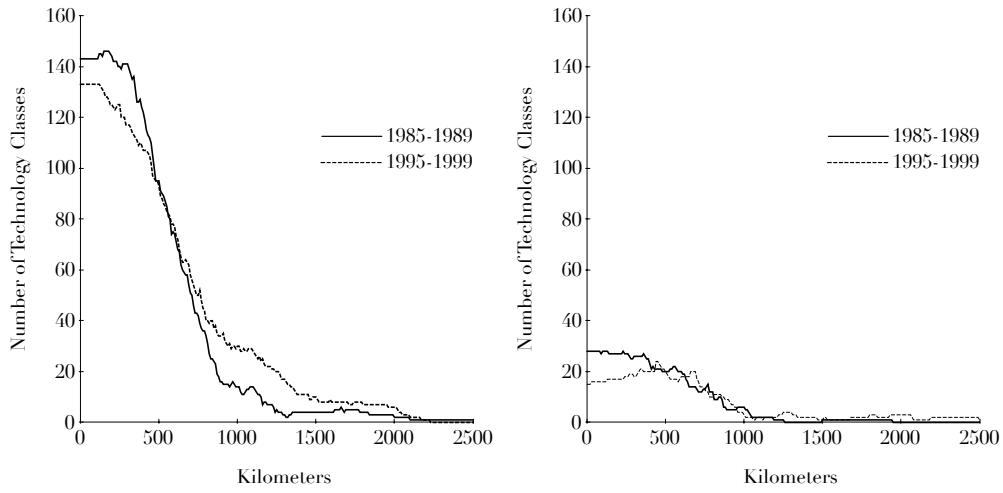
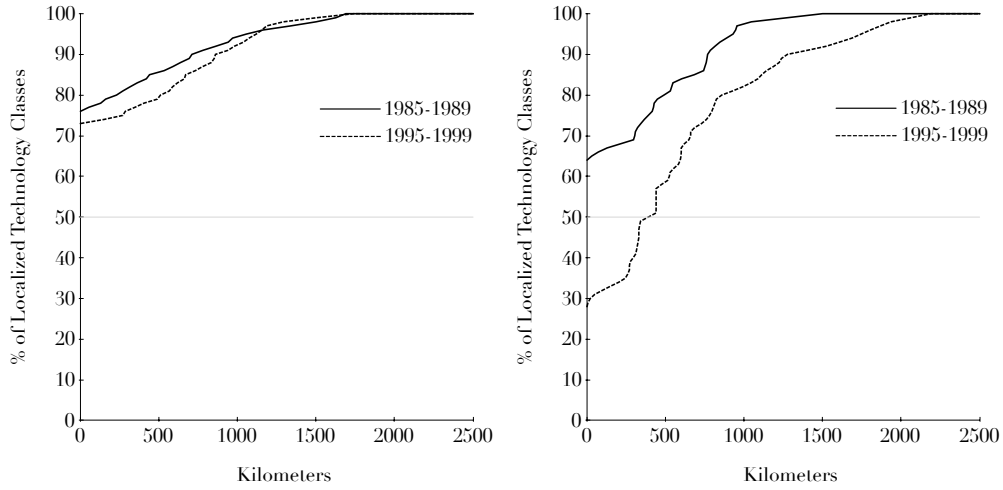


Figure 6: Distance Distribution of $|L_0^1(d)|$ for Six-digit Controls



(a) three-digit controls: $|L^1(d)|$

(b) six-digit controls: $|L^1(d)|$



(c) three-digit controls: Percentage of localized classes

(d) six-digit controls: Percentage of localized classes

Figure 7: Changes in Localization Distances